

第4回講義 資料1

(資料4—①)

(Q4-5—8) $(1, 1)$ を算出で分解した19通りを加法によって確認せよ。

(算出1) $(1, 1) = (2, 1) + (3, 1)$

(算出2) $(1, 1) = (2, 1) + (4, 1) + (13, 1)$

(算出3) $(1, 1) = (2, 1) + (5, 1) + (8, 1)$

(算出4) $(1, 1) = (3, 1) + (3, 1) + (7, 1)$

(算出5) $(1, 1) = (2, 1) + (4, 1) + (14, 1) + (183, 1)$

(算出6) $(1, 1) = (2, 1) + (4, 1) + (15, 1) + (98, 1)$

(算出7) $(1, 1) = (2, 1) + (4, 1) + (18, 1) + (47, 1)$

(算出8) $(1, 1) = (2, 1) + (4, 1) + (23, 1) + (30, 1)$

(算出9) $(1, 1) = (2, 1) + (5, 1) + (9, 1) + (73, 1)$

(算出10) $(1, 1) = (2, 1) + (5, 1) + (13, 1) + (21, 1)$

(算出11) $(1, 1) = (2, 1) + (6, 1) + (7, 1) + (68, 1)$

(算出12) $(1, 1) = (2, 1) + (6, 1) + (8, 1) + (31, 1)$

(算出13) $(1, 1) = (2, 1) + (7, 1) + (8, 1) + (18, 1)$

(算出14) $(1, 1) = (3, 1) + (3, 1) + (8, 1) + (57, 1)$

(算出15) $(1, 1) = (3, 1) + (3, 1) + (9, 1) + (32, 1)$

(算出16) $(1, 1) = (3, 1) + (3, 1) + (12, 1) + (17, 1)$

(算出17) $(1, 1) = (3, 1) + (4, 1) + (5, 1) + (47, 1)$

(算出18) $(1, 1) = (3, 1) + (4, 1) + (7, 1) + (13, 1)$

(算出19) $(1, 1) = (3, 1) + (5, 1) + (7, 1) + (8, 1)$

$$(a,b) + (c,d) = (ac - bd, bc + ad) \text{ より}$$

$$\text{(算出1)} \quad (1, 1) = (2, 1) + (3, 1)$$

$$\begin{aligned} \text{右辺} &= (6-1, 3+2) = (5, 5) \\ &= (1, 1) \end{aligned}$$

$$\text{(算出2)} \quad (1, 1) = (2, 1) + (4, 1) + (13, 1)$$

$$\begin{aligned} \text{右辺} &= (8-1, 4+2) = (6, 6) \\ &= (1, 1) \end{aligned}$$

$$\text{(算出3)} \quad (1, 1) = (2, 1) + (5, 1) + (8, 1)$$

$$\begin{aligned} \text{右辺} &= (10-1, 5+2) + (8, 1) = (9, 7) + (8, 1) \\ &= (72-7, 56+7) = (65, 65) \\ &= (1, 1) \end{aligned}$$

$$\text{(算出4)} \quad (1, 1) = (3, 1) + (3, 1) + (7, 1)$$

$$\begin{aligned} \text{右辺} &= (9-1, 3+3) + (7, 1) = (8, 6) + (7, 1) \\ &= (56-6, 8+42) = (50, 50) \\ &= (1, 1) \end{aligned}$$

$$\text{(算出5)} \quad (1, 1) = (2, 1) + (4, 1) + (14, 1) + (183, 1)$$

$$\begin{aligned} \text{右辺} &= (8-1, 2+4) + (14, 1) + (183, 1) \\ &= (7, 6) + (14, 1) + (183, 1) \\ &= (98-6, 84+7) + (183, 1) = (92, 91) + (183, 1) \\ &= (16836-91, 16653+92) = (16745, 16745) \\ &= (1, 1) \end{aligned}$$

$$\text{(算出6)} \quad (1, 1) = (2, 1) + (4, 1) + (15, 1) + (98, 1)$$

$$\begin{aligned} \text{右辺} &= (8-1, 4+2) + (15, 1) + (98, 1) \\ &= (7, 6) + (15, 1) + (98, 1) \\ &= (105-6, 90+7) + (98, 1) = (99, 97) + (98, 1) \\ &= (9702-97, 99+9506) = (9605, 9605) \\ &= (1, 1) \end{aligned}$$

$$\text{(算出7)} \quad (1, 1) = (2, 1) + (4, 1) + (18, 1) + (47, 1)$$

$$\begin{aligned} \text{右辺} &= (8-1, 4+2) + (18, 1) + (47, 1) \\ &= (7, 6) + (18, 1) + (47, 1) \\ &= (126-6, 108+7) + (47, 1) = (120, 115) + (47, 1) \\ &= (5640-115, 5405+120) = (5525, 5525) \\ &= (1, 1) \end{aligned}$$

- (算出8) $(1, 1) = (2, 1) + (4, 1) + (23, 1) + (30, 1)$
 右边 $= (8-1, 4+2) + (23, 1) + (30, 1)$
 $= (7, 6) + (23, 1) + (30, 1)$
 $= (161-6, 138+7) + (30, 1) = (155, 145) + (30, 1)$
 $= (4650-145, 4350+155) = (4505, 4505)$
 $= (1, 1)$
- (算出9) $(1, 1) = (2, 1) + (5, 1) + (9, 1) + (73, 1)$
 右边 $= (10-1, 5+2) + (9, 1) + (73, 1)$
 $= (9, 7) + (9, 1) + (73, 1)$
 $= (81-7, 63+9) + (73, 1) = (74, 72) + (73, 1)$
 $= (5402-72, 5256+74) = (5330, 5330)$
 $= (1, 1)$
- (算出10) $(1, 1) = (2, 1) + (5, 1) + (13, 1) + (21, 1)$
 右边 $= (10-1, 5+2) + (13, 1) + (21, 1)$
 $= (9, 7) + (13, 1) + (21, 1)$
 $= (117-7, 91+9) + (21, 1) = (110, 100) + (21, 1)$
 $= (2310-100, 2100+110) = (2210, 2210)$
 $= (1, 1)$
- (算出11) $(1, 1) = (2, 1) + (6, 1) + (7, 1) + (68, 1)$
 右边 $= (12-1, 6+2) + (7, 1) + (68, 1)$
 $= (11, 8) + (7, 1) + (68, 1)$
 $= (77-8, 56+11) + (68, 1) = (69, 67) + (68, 1)$
 $= (4692-67, 4556+69) = (4625, 4625)$
 $= (1, 1)$
- (算出12) $(1, 1) = (2, 1) + (6, 1) + (8, 1) + (31, 1)$
 右边 $= (12-1, 6+2) + (8, 1) + (31, 1)$
 $= (11, 8) + (8, 1) + (31, 1)$
 $= (88-8, 64+11) + (31, 1) = (80, 75) + (31, 1)$
 $= (2480-75, 2325+80) = (2405, 2405)$
 $= (1, 1)$
- (算出13) $(1, 1) = (2, 1) + (7, 1) + (8, 1) + (18, 1)$
 右边 $= (14-1, 7+2) + (8, 1) + (18, 1)$
 $= (13, 9) + (8, 1) + (18, 1)$
 $= (104-9, 72+13) + (18, 1) = (95, 85) + (18, 1)$
 $= (1710-85, 1530+95) = (1625, 1625)$
 $= (1, 1)$

$$\text{(算出14)} \quad (1, 1) = (3, 1) + (3, 1) + (8, 1) + (57, 1)$$

$$\begin{aligned} \text{右边} &= (9-1, 3+3) + (8, 1) + (57, 1) \\ &= (8, 6) + (8, 1) + (57, 1) \\ &= (64-6, 48+8) + (57, 1) = (58, 56) + (57, 1) \\ &= (3306-56, 3192+58) = (3250, 3250) \\ &= (1, 1) \end{aligned}$$

$$\text{(算出15)} \quad (1, 1) = (3, 1) + (3, 1) + (9, 1) + (32, 1)$$

$$\begin{aligned} \text{右边} &= (9-1, 3+3) + (9, 1) + (32, 1) \\ &= (8, 6) + (9, 1) + (32, 1) \\ &= (72-6, 54+8) + (32, 1) = (66, 62) + (32, 1) \\ &= (2112-62, 1984+66) = (2050, 2050) \\ &= (1, 1) \end{aligned}$$

$$\text{(算出16)} \quad (1, 1) = (3, 1) + (3, 1) + (12, 1) + (17, 1)$$

$$\begin{aligned} \text{右边} &= (9-1, 3+3) + (12, 1) + (17, 1) \\ &= (8, 6) + (12, 1) + (17, 1) \\ &= (96-6, 72+8) + (17, 1) = (90, 80) + (17, 1) \\ &= (1530-80, 1360+90) = (1450, 1450) \\ &= (1, 1) \end{aligned}$$

$$\text{(算出17)} \quad (1, 1) = (3, 1) + (4, 1) + (5, 1) + (47, 1)$$

$$\begin{aligned} \text{右边} &= (12-1, 4+3) + (5, 1) + (47, 1) \\ &= (11, 7) + (5, 1) + (47, 1) \\ &= (55-7, 35+11) + (47, 1) = (48, 46) + (47, 1) \\ &= (2256-46, 2162+48) = (2210, 2210) \\ &= (1, 1) \end{aligned}$$

$$\text{(算出18)} \quad (1, 1) = (3, 1) + (4, 1) + (7, 1) + (13, 1)$$

$$\begin{aligned} \text{右边} &= (12-1, 4+3) + (7, 1) + (13, 1) \\ &= (11, 7) + (7, 1) + (13, 1) \\ &= (77-7, 49+11) + (13, 1) = (70, 60) + (13, 1) \\ &= (910-60, 780+70) = (850, 850) \\ &= (1, 1) \end{aligned}$$

$$\text{(算出19)} \quad (1, 1) = (3, 1) + (5, 1) + (7, 1) + (8, 1)$$

$$\begin{aligned} \text{右边} &= (15-1, 5+3) + (7, 1) + (8, 1) \\ &= (14, 8) + (7, 1) + (8, 1) \\ &= (98-8, 56+14) + (8, 1) = (90, 70) + (8, 1) \\ &= (720-70, 560+90) = (650, 650) \\ &= (1, 1) \end{aligned}$$